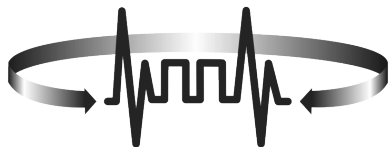


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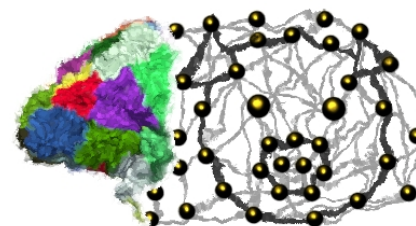
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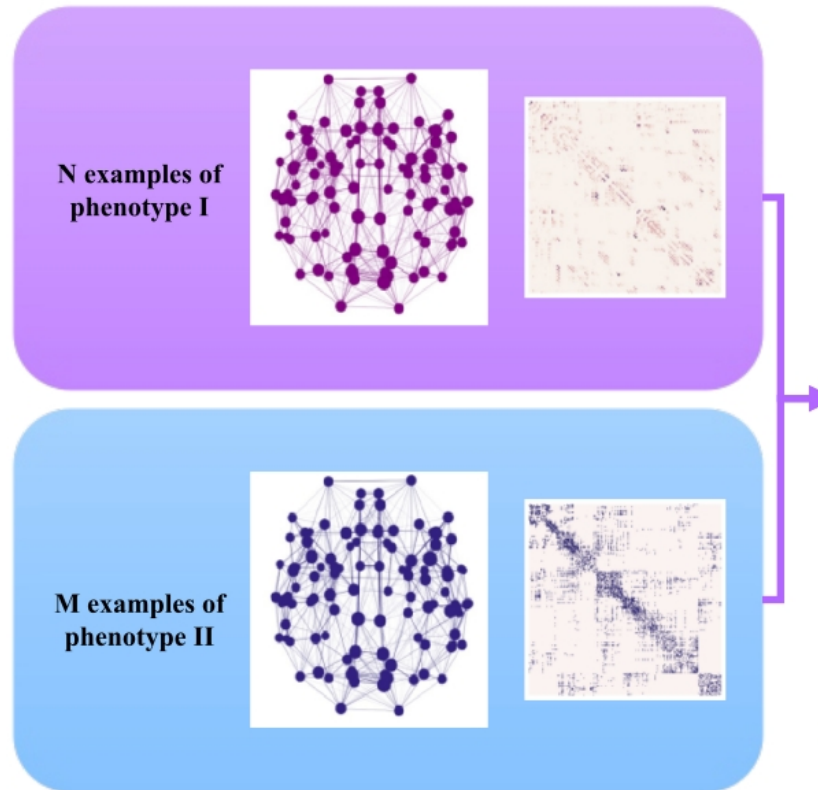
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Kernel Classification of Connectomes Based on Earth Mover's Distance between Graph Spectra

Yulia Dodonova, Mikhail Belyaev, Anna Tkachev,
Dmitry Petrov, Leonid Zhukov



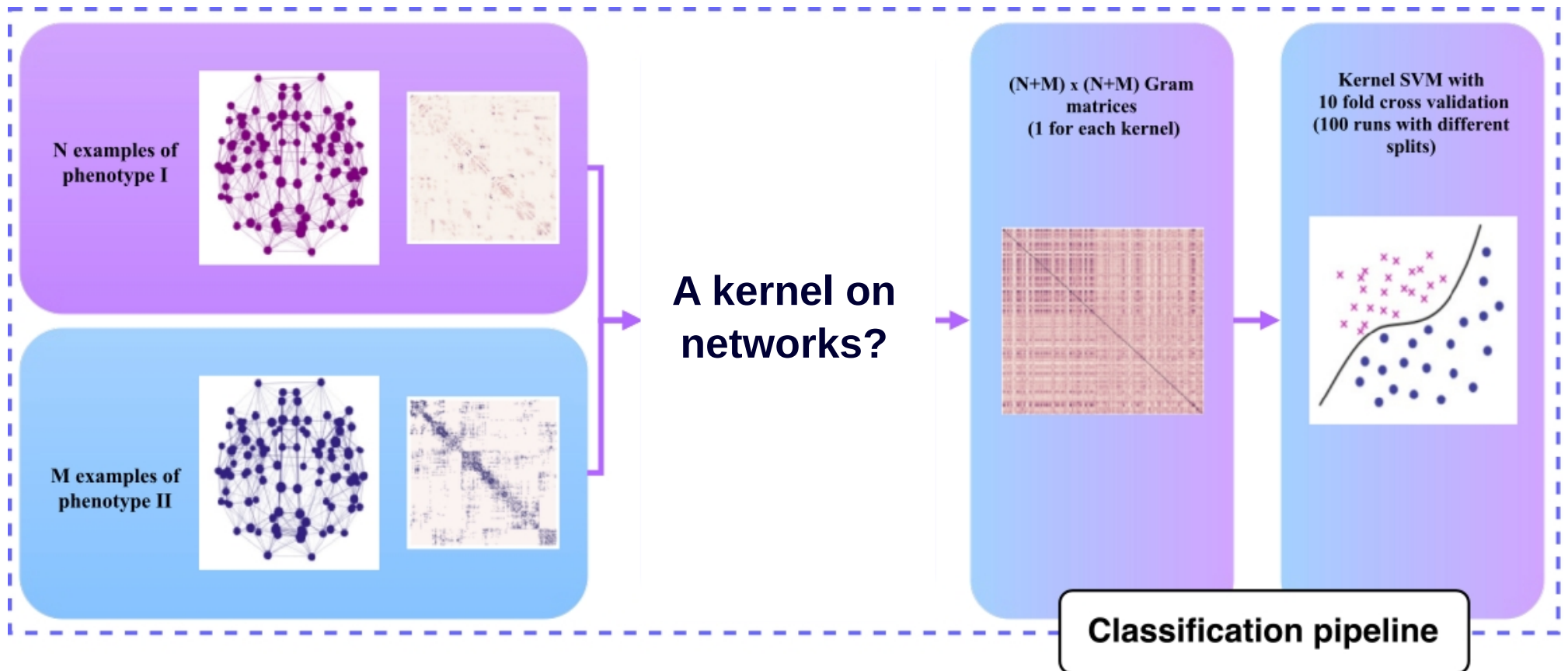
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How to classify networks?

- Graph embedding methods
 - describe a network via a vector
- Kernel classifiers
 - define a positive semi-definite function on graphs and feed it to the SVM (support vector machines)

Kernel approach



A kernel on networks?

Provided we have a distance between the two networks G_1 and G_2 , we can compute a kernel by:

$$K(G, G') = e^{-\alpha\omega(G, G')}$$

**How to compute a distance
between two connectomes?**

Idea

Use spectral distributions
of the normalized graph Laplacians
to capture differences
in the structure of connectomes

What is a normalized Laplacian?

Let A be a graph adjacency matrix

D is a diagonal matrix of weighted node degrees:

$$d_i = \sum_j a_{ij}$$

Graph Laplacian is:

$$L = D - A$$

Normalized graph Laplacian is:

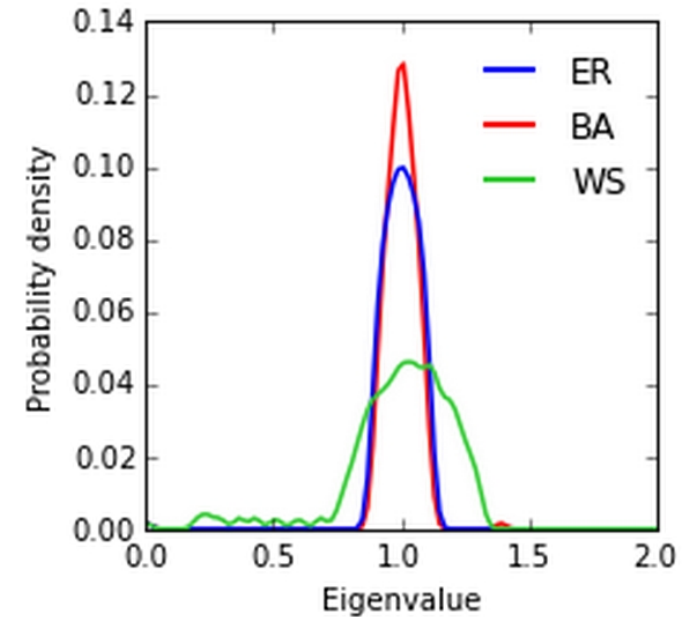
$$\mathcal{L} = D^{-1/2} L D^{-1/2}$$

Why its spectra are so special?

The eigenvalues are in range from 0 to 2:

- can compare networks with different sizes
- no need to normalize networks

The shape of the eigenvalue distribution, its symmetry and the multiplicity of particular values capture information about graph structure



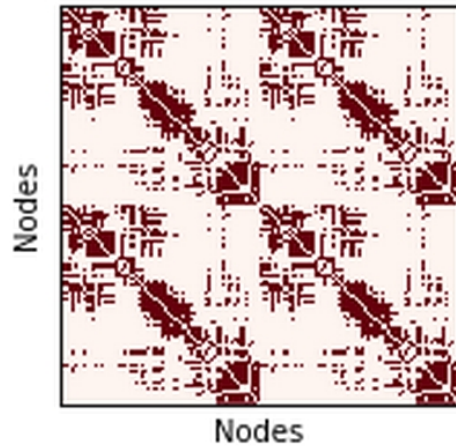
Spectral distributions of random graphs (Erdős-Rényi, Barabási-Albert, Watts-Strogatz)

Chung F. (1997) Spectral Graph Theory

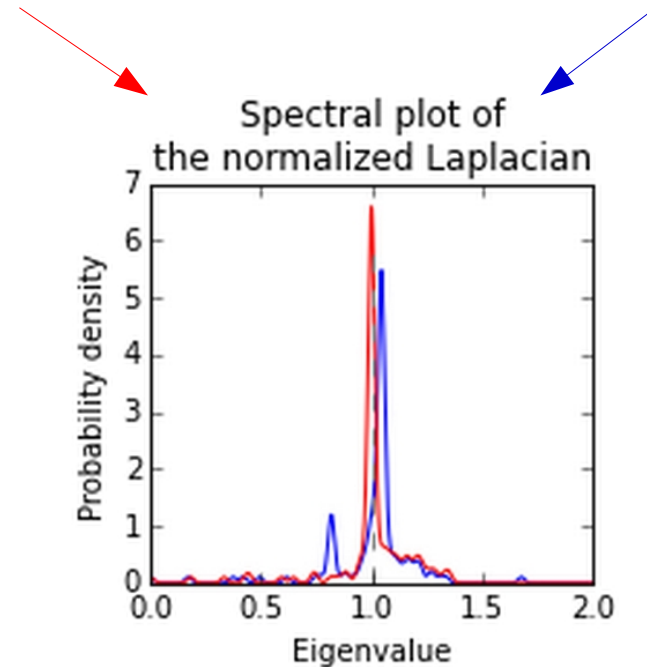
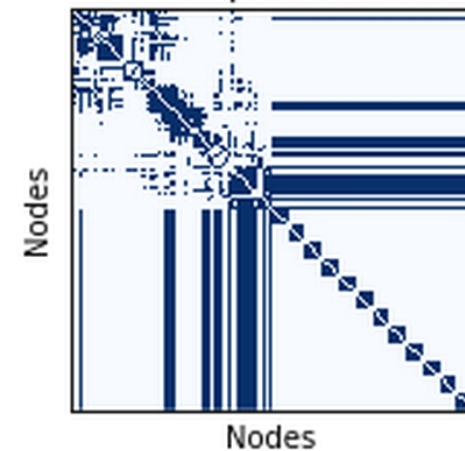
Banerjee A., Jost J. (2008) Spectral plot properties: towards a qualitative classification of networks. Networks and heterogeneous media, 3, 2, 395–411

Graph structure in spectral distributions

Adjacency matrix
with each vertex doubled



Adjacency matrix
with cliques of size 5



de Lange S.C., de Reus M.A., van den Heuvel M.P. (2014) The Laplacian spectrum of neural networks. *Frontiers in Computational Neuroscience*, 1–12

Distance between spectral distributions?

Could use measures from information theory

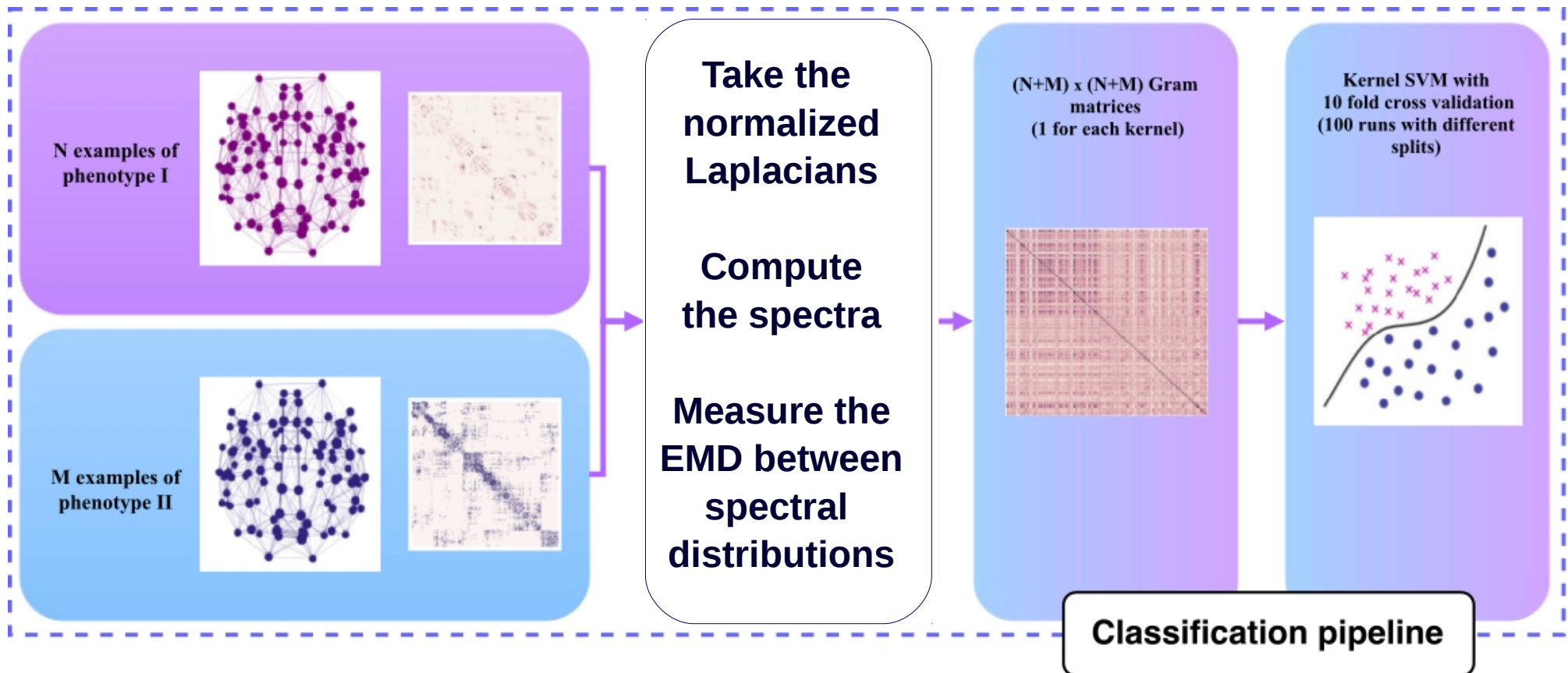
- *need density reconstruction*

An idea behind the earth mover's distance (EMD):

If each distribution is represented by some amount of dirt, EMD is the minimum cost required to move the dirt of one distribution to produce the other. The cost is the amount of dirt moved times the distance by which it is moved.

Rubner, Y. , Tomasi, C., Guibas, L. J.: The earth movers distance as a metric for image retrieval, International Journal of Computer Vision, 40, 2000 (2000)

Pipeline



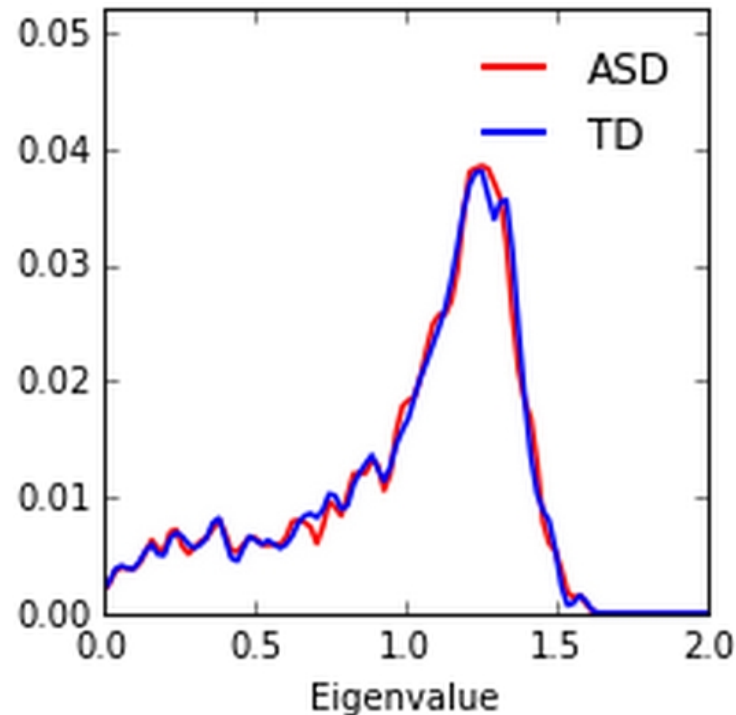
Example dataset: UCLA Autism

- structural connectomes
 - 94 subjects
 - 51 ASD subjects (age 13 ± 2.8 years),
43 TD subjects (age 13.1 ± 2.4 years)
 - 264x264 matrices
- deterministic tractography (FACT)

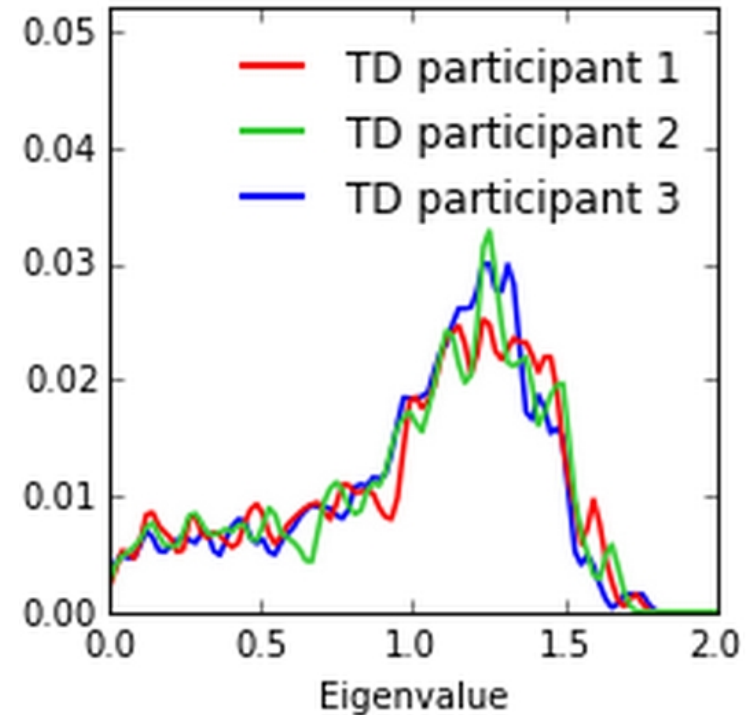
Rudie, J.D., Brown, J.A., Beck-Pancer, D., Hernandez, L.M., Dennis, E.L., Thompson, P.M., et al.: Altered functional and structural brain network organization in autism. Neuroimage Clin 2, 79–94 (2013)

Brown, J.A., Rudie, J.D., Bandrowski, A., Van Horn, J.D., Bookheimer, S.Y. (2012) The UCLA multimodal connectivity database: a web-based platform for brain connectivity matrix sharing and analysis. Frontiers in Neuroinformatics 6, 28.

UCLA Autism: spectral distributions



Spectra of the
group average
matrices

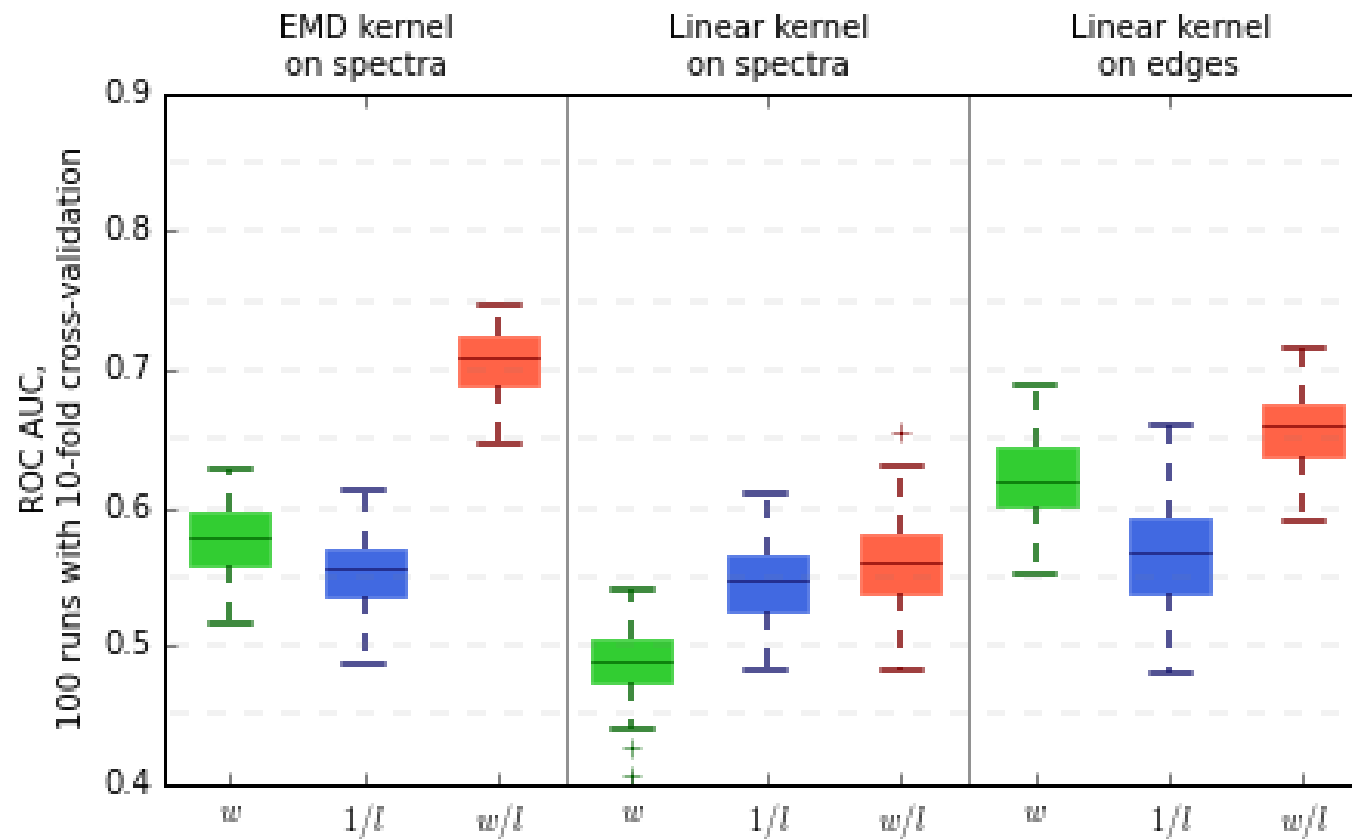


Spectra of the
individual matrices
of TD class

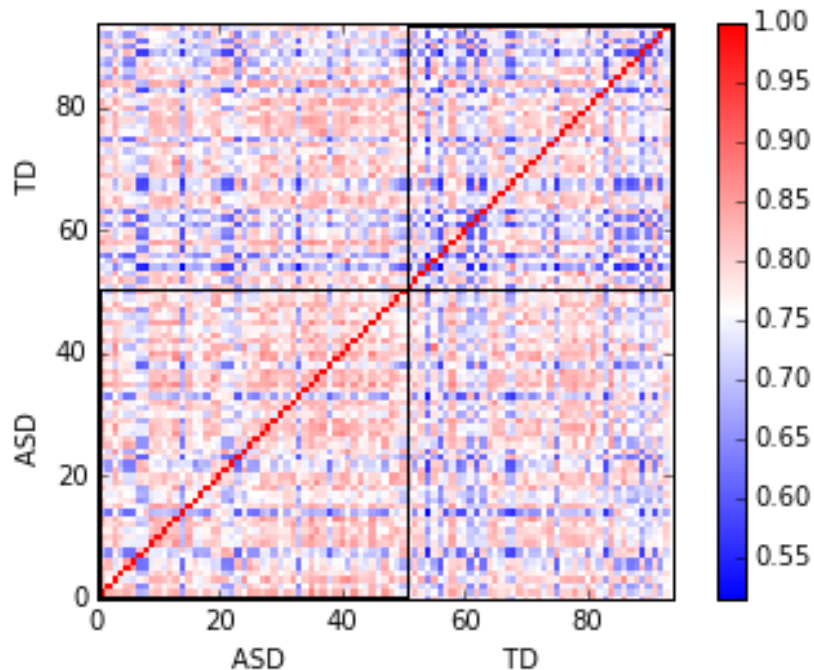
UCLA Autism: classification

- Run parallel analysis on connectomes with three different weighting schemes:
 - weights proportional to the number of streamlines
 - weights proportional to the inverse Euclidean distance between the centers of the respective regions
 - combined the above weights
- Compare performance of the proposed pipeline against the linear SVM classifiers on the vectors of edges and the vectors of sorted eigenvalues
- Area under the ROC-curve (ROC AUC),
10-fold cross-validation, 100 runs with different splits

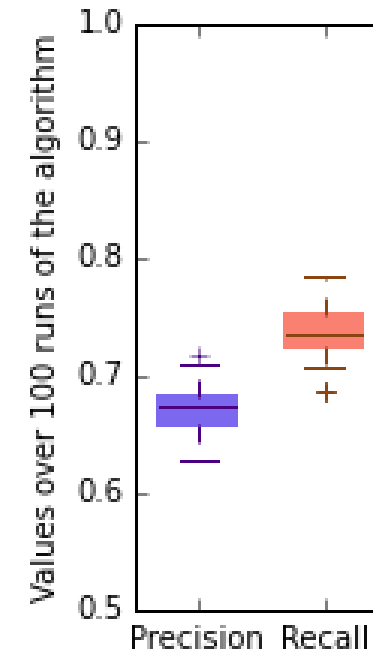
UCLA Autism: results



UCLA Autism: results



Gram matrix based on the EMD between the normalized Laplacian spectra: the TD group shows larger variability



Precision and recall values:
Algorithm performs quite well
Identifying ASD subjects, but tends to classify TD subjects as pathological

Conclusions

- Spectral distributions of the normalized Laplacians capture some meaningful **structural properties** of brain networks which make them different from other network classes
- Spectral distributions of connectomes can help to **distinguish normal and pathological brain networks**
- **Further studies are needed** to explore whether these findings generalize to other classification tasks and other schemes of network construction



Thank you!



Q?



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